

6.3

Angles of Polygons

For use with Exploration 6.3

Essential Question What is the sum of the measures of the interior angles of a polygon?

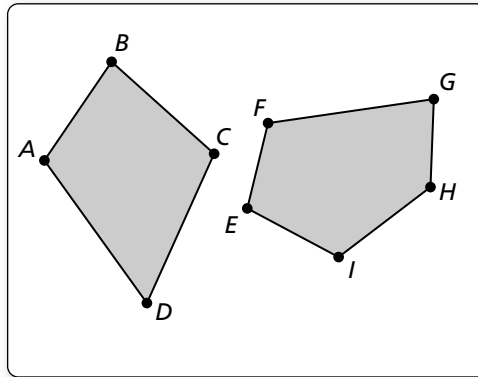
1 EXPLORATION: The Sum of the Angle Measures of a Polygon

Go to *BigIdeasMath.com* for an interactive tool to investigate this exploration.

Work with a partner. Use dynamic geometry software.

- a. Draw a quadrilateral and a pentagon. Find the sum of the measures of the interior angles of each polygon.

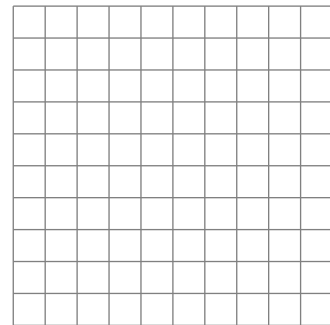
Sample



- b. Draw other polygons and find the sums of the measures of their interior angles. Record your results in the table below.

Number of sides, n	3	4	5	6	7	8	9
Sum of angle measures, S							

- c. Plot the data from your table in a coordinate plane.



- d. Write a function that fits the data. Explain what the function represents.

6.3 Angles of Polygons (continued)**2 EXPLORATION: Measure of One Angle in a Regular Polygon**

Go to *BigIdeasMath.com* for an interactive tool to investigate this exploration.

Work with a partner.

- Use the function you found in Exploration 1 to write a new function that gives the measure of one interior angle in a regular polygon with n sides.
- Use the function in part (a) to find the measure of one interior angle of a regular pentagon. Use dynamic geometry software to check your result by constructing a regular pentagon and finding the measure of one of its interior angles.
- Copy your table from Exploration 1 and add a row for the measure of one interior angle in a regular polygon with n sides. Complete the table. Use dynamic geometry software to check your results.

Number of sides, n	3	4	5	6	7	8	9
Sum of angle measures, S							
Measure of one interior angle							

Communicate Your Answer

- What is the sum of the measures of the interior angles of a polygon?
- Find the measure of one interior angle in a regular dodecagon (a polygon with 12 sides).

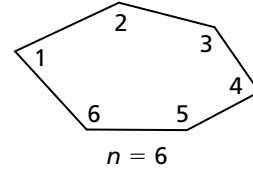
6.3**Practice**

For use after Lesson 6.3

Theorems**Polygon Interior Angles Theorem**

The sum of the measures of the interior angles of a convex n -gon is $(n - 2) \cdot 180^\circ$.

$$m\angle 1 + m\angle 2 + \cdots + m\angle n = (n - 2) \cdot 180^\circ$$

**Notes:****Corollary to the Polygon Interior Angles Theorem**

The sum of the measures of the interior angles of a quadrilateral is 360° .

Notes:

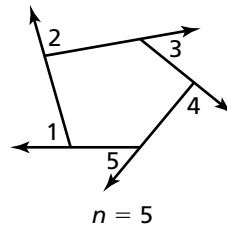
6.3 Practice (continued)

Polygon Exterior Angles Theorem

The sum of the measures of the exterior angles of a convex polygon, one angle at each vertex, is 360° .

$$m\angle 1 + m\angle 2 + \dots + m\angle n = 360^\circ$$

Notes:



Worked-Out Examples

Example #1

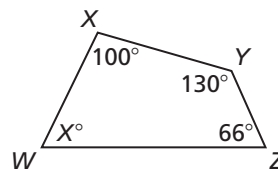
Find the value of x .

$XYZW$ is a quadrilateral, therefore the sum of the measures of the interior angles is $(4 - 2) \cdot 180^\circ = 360^\circ$.

$$100^\circ + 130^\circ + 66^\circ + x^\circ = 360^\circ$$

$$296 + x = 360$$

$$x = 64$$



Example #2

Find the measures of $\angle X$ and $\angle Y$.

The polygon has 6 sides, therefore the sum of the measures of the interior angles is $(6 - 2) \cdot 180^\circ = 720^\circ$.

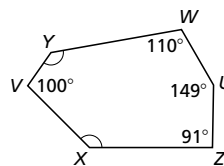
$$100^\circ + x^\circ + 110^\circ + 149^\circ + 91^\circ + x^\circ = 720^\circ$$

$$2x + 450 = 720$$

$$2x = 270$$

$$x = 135$$

$$m\angle X = m\angle Y = 135^\circ$$



6.3 Practice (continued)

Practice A

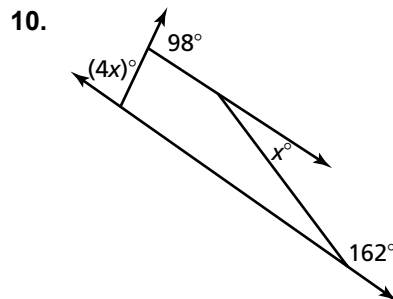
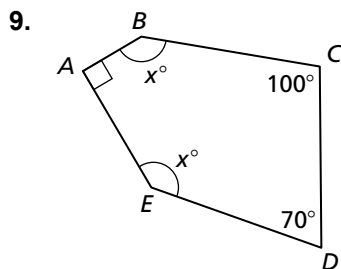
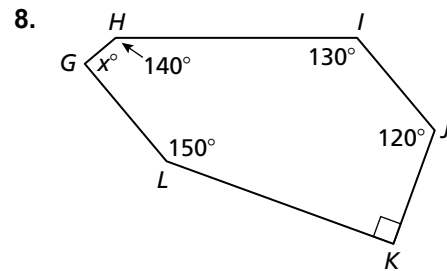
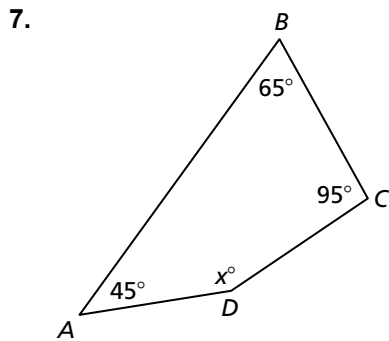
In Exercises 1–3, find the sum of the measures of the interior angles of the indicated convex polygon.

1. octagon 2. 15-gon 3. 24-gon

In Exercises 4–6, the sum of the measures of the interior angles of a convex polygon is given. Classify the polygon by the number of sides.

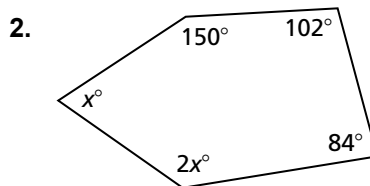
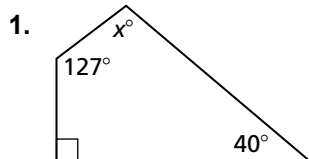
4. 900° 5. 1620° 6. 2880°

In Exercises 7–10, find the value of x .

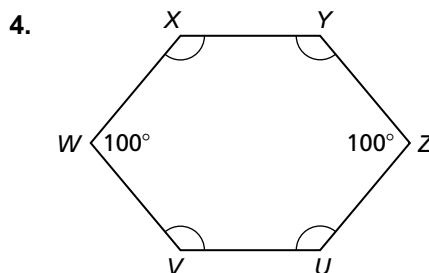
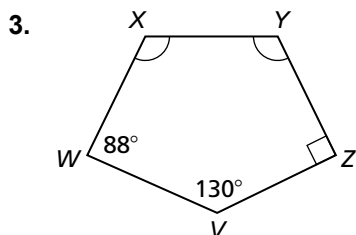


Practice B

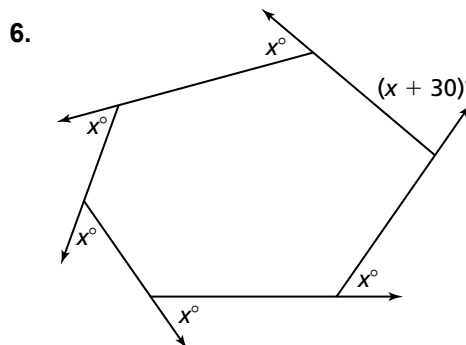
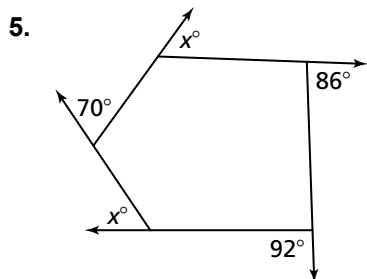
In Exercises 1 and 2, find the value of x .



In Exercises 3 and 4, find the measures of $\angle X$ and $\angle Y$.



In Exercises 5 and 6, find the value of x .



7. Find the measure of each interior angle and each exterior angle of a regular 24-gon.
8. Each exterior angle of a regular polygon has a measure of 18° . Find the number of sides of the regular polygon.
9. A polygon has two pairs of complementary interior angles and three sets of supplementary interior angles. The sum of the remaining interior angles is 1440° . How many sides does the polygon have? Explain.
10. The figure shows interior angle measures of the kite.
 - a. Find the sum of the measures of the interior angles of the convex polygon.
 - b. Find the value of x .

