### 9.3 Input-Output Jables

STATE STANDARDS

MA.6.A.3.3
MA.6.A.3.6

## Essential Question

How can you use a table to describe a function?

## 1 ACTIVIJY: Using a Function Table

## Work with a partner.

a. Copy and complete the table for the perimeter of the rectangle.


| Input, $\boldsymbol{x}$ | 1 | 2 | 3 | 4 | 5 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Output, $\boldsymbol{P}$ |  |  |  |  |  |

b. Write an equation that describes the function.
c. Use your equation to find the value of $x$ for which the perimeter is 50 .

## 2 AcJIVJIY: Using a Function Table

Work with a partner. Use the strategy shown in Activity 1 to make a table that shows the pattern for the area. Write an equation that describes the function. Then use your equation to find which figure has an area of 81 .
a.


Figure 1


Figure 2


Figure 3


Figure 4
b.


Figure 1


Figure 2


Figure 3


Figure 4

## 3 ACTIVIJY: Making a Function Table

Work with a partner. Copy and complete a sales tax table for each of the four counties.

Collier County, 6.00\%

| Sale, $\boldsymbol{x}$ | $\$ 20$ | $\$ 30$ | $\$ 40$ | $\$ 50$ | $\$ 60$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Sales Tax, $\boldsymbol{T}$ |  |  |  |  |  |

Hernando County, 6.50\%

| Sale, $\boldsymbol{x}$ | $\$ 20$ | $\$ 30$ | $\$ 40$ | $\$ 50$ | $\$ 60$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Sales Tax, $\boldsymbol{T}$ |  |  |  |  |  |

Columbia County, 7.00\%

| Sale, $\boldsymbol{x}$ | $\$ 20$ | $\$ 30$ | $\$ 40$ | $\$ 50$ | $\$ 60$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Sales Tax, $\boldsymbol{T}$ |  |  |  |  |  |

Escambia County, 7.50\%

| Sale, $\boldsymbol{x}$ | $\$ 20$ | $\$ 30$ | $\$ 40$ | $\$ 50$ | $\$ 60$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Sales Tax, $\boldsymbol{T}$ |  |  |  |  |  |

## What Is Your Answer?

4. IN YOUR OWN WORDS How can you use a table to describe a function? Describe an example of a function table in real life.

| Amount of Sale | Tax |
| :--- | :---: |
| $.10-.16$ | .01 |
| $.17-.33$ | .02 |
| $.34-.50$ | .03 |
| $.51-.66$ | .04 |
| $.67-.83$ | .05 |
| $.84-1.09$ | .06 |


"Dear Sir: Yesterday, I bought a piece of 9-cent candy six times and paid NO tax. Today, I bought six pieces at once and you charged me \$0.04 tax. What's going on?"

## Key Vocabulary

 input-output table, p. 380
## Input-Output Tables

A function can be represented by an input-output table. The table below is for the function $y=x+2$.


## EXAMPLE (1) Completing Input-Output Tables

Write an equation for the function. Then copy and complete the table.
a. The output is $\mathbf{1}$ less than the input.

| Input, $\boldsymbol{x}$ | 2 | 3 | 4 | 5 |
| :--- | :---: | :---: | :---: | :---: |
| Output, $\boldsymbol{y}$ |  |  |  |  |

b. The output is twice the input.

| Input, $\boldsymbol{x}$ | 0 | 3 | 6 | 9 |
| :--- | :--- | :--- | :--- | :--- |
| Output, $\boldsymbol{y}$ |  |  |  |  |

a. An equation is $y=x-1$.

b. An equation is $y=2 x$.


Now You're Ready
Exercises 5 and 6

Write an equation for the function. Then copy and complete the table.

1. The output is 5 more than the input.

| Input, $\boldsymbol{x}$ | 1 | 3 | 5 | 7 |
| :--- | :--- | :--- | :--- | :--- |
| Output, $\boldsymbol{y}$ |  |  |  |  |

2. The output is the product of 7 and the input.

| Input, $\boldsymbol{x}$ | 0 | 2 | 4 | 6 |
| :--- | :--- | :--- | :--- | :--- |
| Output, $\boldsymbol{y}$ |  |  |  |  |

## EXAMPLE

## 2 Standardized Test Practice

Which function rule is shown by the table?
(A) $y=5 x$
(B) $y=\frac{x}{5}$
(C) $y=x+4$
(D) $y=10 x$

Look at the relationship between the inputs and outputs. Each output $y$ is 5 times the input $x$. So, the function rule is $y=5 x$.

| Input, $\boldsymbol{x}$ | Output, $\boldsymbol{y}$ |
| :---: | :---: |
| 1 | 5 |
| 2 | 10 |
| 4 | 20 |
| 8 | 40 |

$\therefore$ The correct answer is (A).

EXAMPLE

| Input, $\boldsymbol{x}$ | Output, $\boldsymbol{y}$ |
| :---: | :---: |
| 1 | 7 |
| 5 | 15 |
| 10 | 25 |
| 20 | 45 |
| $?$ | 53 |

Step 2: Substitute 53 for $y$. Then solve for $x$.

$$
\begin{aligned}
y & =5+2 x & & \text { Write the equation. } \\
53 & =5+2 x & & \text { Substitute } 53 \text { for } y . \\
48 & =2 x & & \text { Subtract } 5 \text { from each side. } \\
24 & =x & & \text { Divide each side by } 2 .
\end{aligned}
$$

## Check

$$
\begin{aligned}
2 x+5 & =53 \\
2(24)+5 & \stackrel{?}{=} 53 \\
48+5 & \stackrel{?}{=} 53 \\
53 & =53
\end{aligned}
$$

$\therefore$ The missing input is 24 .

## On Your Own

Exercises 7-13

Use the first three input values to write an equation for the function shown by the table. Then find the missing input.
3.

| Input, $\boldsymbol{x}$ | Output, $\boldsymbol{y}$ |
| :---: | :---: |
| 1 | 5 |
| 3 | 7 |
| 7 | 11 |
| $?$ | 25 |

4. 

| Input, $\boldsymbol{x}$ | Output, $\boldsymbol{y}$ |
| :---: | :---: |
| 2 | 1 |
| 4 | 2 |
| 6 | 3 |
| $?$ | 4 |

## Vocabulary and Concept Check

1. VOCABULARY Explain how you can use an input-output table to represent a function.
2. DIFFERENT WORDS, SAME QUESTION Which is different? Find "both" answers.

What output is 4 more than twice the input 3 ?

What output is the sum of 2 times the input 3 and 4 ?

What output is twice the sum of the input 3 and 4 ?

What output is 4 increased by twice the input 3 ?

## Practice and Problem Solving

Copy and complete the input-output table for the function.
3. $y=x+5$

| Input, $\boldsymbol{x}$ | 1 | 2 | 3 | 4 |
| :--- | :--- | :--- | :--- | :--- |
| Output, $\boldsymbol{y}$ |  |  |  |  |

4. $y=4 x$

| Input, $\boldsymbol{x}$ | 0 | 2 | 4 | 6 |
| :--- | :--- | :--- | :--- | :--- |
| Output, $\boldsymbol{y}$ |  |  |  |  |

Write an equation for the function. Then copy and complete the table.
5. The output is 3 more than the input.

| Input, $\boldsymbol{x}$ | 0 | 1 | 2 | 3 |
| :--- | :--- | :--- | :--- | :--- |
| Output, $\boldsymbol{y}$ |  |  |  |  |

6. The output is 5 times the input.

| Input, $\boldsymbol{x}$ | 1 | 3 | 5 | 7 |
| :--- | :--- | :--- | :--- | :--- |
| Output, $\boldsymbol{y}$ |  |  |  |  |

## Write an equation for the function shown by the table.

7. 

| Input, $\boldsymbol{x}$ | 1 | 2 | 3 | 4 |
| :--- | :---: | :---: | :---: | :---: |
| Output, $\boldsymbol{y}$ | 9 | 10 | 11 | 12 |

9. 

| Input, $\boldsymbol{x}$ | 0 | 3 | 6 | 9 |
| :--- | :--- | :--- | :--- | :--- |
| Output, $\boldsymbol{y}$ | 0 | 1 | 2 | 3 |

10. 

| Input, $\boldsymbol{x}$ | 2 | 4 | 6 | 8 |
| :--- | :---: | :---: | :---: | :---: |
| Output, $\boldsymbol{y}$ | 4 | 8 | 12 | 16 |


| Input, $\boldsymbol{x}$ | 3 | 5 | 7 | 9 |
| :--- | :--- | :--- | :--- | :--- |
| Output, $\boldsymbol{y}$ | 1 | 3 | 5 | 7 |

11. ERROR ANALYSIS Describe and correct the error in writing an equation for the function shown by the table.


| Input, $\boldsymbol{x}$ | 0 | 4 | 8 | 12 |
| :--- | :---: | :---: | :---: | :---: |
| Output, $\boldsymbol{y}$ | 0 | 1 | 2 | 3 |

$y=4 x$

In Exercises 12 and 13, copy and complete the table.
12. For each output, multiply the input by 4 , then subtract 5 .

| Input, $\boldsymbol{x}$ | 2 | 3 | 4 | 7 |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Output, $\boldsymbol{y}$ | 3 | 7 | 11 | 23 | 35 | 55 |

13. For each output, divide the input by 2 , then add 4.

| Input, $\boldsymbol{x}$ |  | 2 | 4 | 10 |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Output, $\boldsymbol{y}$ | 4 | 5 | 6 | 9 | 12 | 17 |

14. FLORIDA KEYS You travel along US Highway 1 from mile marker 0 in Key West to mile marker 100 in Key Largo.

a. Copy and complete the input-output table.

| Distance from Key West, $\boldsymbol{x}$ | 0 | 30 | 47 | 82 | 100 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Distance to Key Largo, $\boldsymbol{y}$ |  |  |  |  |  |


b. Write a function rule in which $x$ is the input and $y$ is the output.
c. Can you use your function rule to find the distance to Florida City? If not, write a function rule that you can use.
15. TIME Make an input-output table with the Greenwich Mean Time (GMT) hourly times as inputs, and times where you live as outputs. Write a function rule for the data.
16.
 $x=0,1,2,3$, and 4 .

## Fair Game Review what you learned in previous grades \& lessons

Plot the ordered pairs in the same coordinate plane. SKILLS REVIEW HANDBOOK
17. $(1,2)$
18. $(0,7)$
19. $(2,3)$
20. $(6,5)$
21. MULTIPLE CHOICE Which is the solution of the inequality $6 x \leq 24$ ?

## SECTION 8.3

(A) $x<4$
(B) $x \leq 4$
(C) $x<144$
(D) $x \leq 144$

