

9.6b Scientific Notation

To add or subtract numbers written in scientific notation with the same power of 10, add or subtract the factors.

EXAMPLE 1 Adding Numbers Written in Scientific Notation

Find $(4.6 \times 10^3) + (8.72 \times 10^3)$. Write your answer in scientific notation.

$$\begin{aligned}(4.6 \times 10^3) + (8.72 \times 10^3) \\ &= (4.6 + 8.72) \times 10^3 && \text{Distributive Property} \\ &= 13.32 \times 10^3 && \text{Add.} \\ &= (1.332 \times 10^1) \times 10^3 && \text{Write 13.32 in scientific notation.} \\ &= 1.332 \times 10^4 && \text{Product of Powers Property}\end{aligned}$$

To add or subtract numbers written in scientific notation with different powers of 10, first rewrite the numbers so they have the same power of 10.

EXAMPLE 2 Subtracting Numbers Written in Scientific Notation

Find $(3.5 \times 10^{-2}) - (6.6 \times 10^{-3})$. Write your answer in scientific notation.

The numbers do not have the same power of 10. Rewrite 6.6×10^{-3} so that it has the same power of 10 as 3.5×10^{-2} .

$$\begin{aligned}6.6 \times 10^{-3} &= 6.6 \times 10^{-1} \times 10^{-2} && \text{Rewrite } 10^{-3} \text{ as } 10^{-1} \times 10^{-2}. \\ &= 0.66 \times 10^{-2} && \text{Rewrite } 6.6 \times 10^{-1} \text{ as } 0.66.\end{aligned}$$

Subtract the factors.

$$\begin{aligned}(3.5 \times 10^{-2}) - (0.66 \times 10^{-2}) \\ &= (3.5 - 0.66) \times 10^{-2} && \text{Distributive Property} \\ &= 2.84 \times 10^{-2} && \text{Subtract.}\end{aligned}$$

Practice

Add or subtract. Write your answer in scientific notation.

- $(3 \times 10^7) + (2.4 \times 10^7)$
- $(7.2 \times 10^{-6}) + (5.44 \times 10^{-6})$
- $(9.2 \times 10^8) - (4 \times 10^8)$
- $(7.8 \times 10^{-5}) - (4.5 \times 10^{-5})$
- $(9.7 \times 10^6) + (6.7 \times 10^5)$
- $(8.2 \times 10^2) + (3.41 \times 10^{-1})$
- $(1.1 \times 10^5) - (4.3 \times 10^4)$
- $(2.4 \times 10^{-1}) - (5.5 \times 10^{-2})$

To divide numbers written in scientific notation, divide the factors and powers of 10 separately.

EXAMPLE 3 Dividing Numbers Written in Scientific Notation

Find $\frac{1.5 \times 10^{-8}}{6 \times 10^7}$. Write your answer in scientific notation.

$$\frac{1.5 \times 10^{-8}}{6 \times 10^7} = \frac{1.5}{6} \times \frac{10^{-8}}{10^7}$$

Rewrite as a product of fractions.

$$= 0.25 \times \frac{10^{-8}}{10^7}$$

Divide 1.5 by 6.

$$= 0.25 \times 10^{-15}$$

Quotient of Powers Property

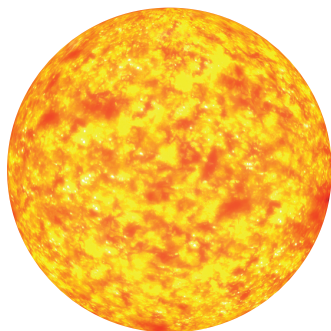
$$= 2.5 \times 10^{-1} \times 10^{-15}$$

Write 0.25 in scientific notation.

$$= 2.5 \times 10^{-16}$$

Product of Powers Property

EXAMPLE 4 Real-Life Application



Diameter = 1.4×10^6 km

How many times greater is the diameter of the Sun than the diameter of Earth?



Diameter = 1.28×10^4 km

Divide the diameter of the Sun by the diameter of Earth.

$$\frac{1.4 \times 10^6}{1.28 \times 10^4} = \frac{1.4}{1.28} \times \frac{10^6}{10^4}$$

Rewrite as a product of fractions.

$$= 1.09375 \times 10^2$$

Divide and use Quotient of Powers Property.

$$= 109.375$$

Write in standard form.

❖ The diameter of the Sun is about 109 times greater than the diameter of Earth.

Practice

Divide. Write your answer in scientific notation.

9. $(6 \times 10^4) \div (3 \times 10^4)$

10. $(2.3 \times 10^7) \div (9.2 \times 10^7)$

11. $(1.5 \times 10^{-3}) \div (7.5 \times 10^2)$

12. $(5.8 \times 10^{-6}) \div (2 \times 10^{-3})$

13. **MONEY** How many times greater is the thickness of a dime than the thickness of a dollar bill?



Thickness = 1.35×10^{-1} cm



Thickness = 1.0922×10^{-2} cm